

Graham Jones

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Chapter 1

Introduction

This describes the implementation the AlloppNET model for arbitrary numbers of diploids, tetraploids, and hybridizations.

The code has been changed quite a bit 2012-05-04 to cater for the extensions. Mainly

- The network is divided into diploid and tetraploid parts differently. See section 1.2.
- The ‘move legs’ MCMC move no longer used, but is replaced by changes to diploid history.
- New move to change the number of hybridizations (ie number of tetraploid trees).
- I no longer use `SimpleTree` to implement the diploid or tetraploid trees.
- I have removed the ‘no diploids’ case.
- In some places I have specialised more to tetraploids (no hexaploids etc).
- In terms of classes, since April/May 2012 `AlloppFootLinks`, `AlloppLegLink`, `AlloppTreeLeg` have disappeared, but `AlloppDiploidHistory` has become more complicated. `AlloppNetworkNodeSlide` has become larger and swallowed `AlloppMoveLegs`. Operators `AlloppChangeNumHybridizations` and `AlloppHybPopSizesScale` added.
- Some unit tests no longer work (or aren’t relevant).

1.1 Jargon

I have started using the words **leg**, **foot**, and **union** to mean special things. Also, I use **diploid history**, **MNL move** and **hyb-tip**.

The species network is composed of homoploid trees, which are joined together. A higher ploidy tree is joined to a lower ploidy tree with one or more **legs**. The point where a leg meets the branch of the lower ploidy tree is a **foot**. In the new (Aug 2012) setup, the feet are represented as **hyb-tips** in the **diploid history**. See section 1.2.

A **union** is a set of indices where each index represents a species, or more often, a species and a sequence. For example, if a, b, c, ... are species, 1, 2, 3, ... are individuals and A, B, C, ... label

sequences, so that a single sequence (taxon) in an alignment might be c2B, then a union can represent a set of elements like {aA, bA, bC}. The identity of individuals 1,2,3, ... is ignored. At a tip in a gene tree, or a tip in the multi-labelled tree, there will be a single species and a single sequence, like aA or bC. At internal nodes, there are sets of them, each one being a union of its children's sets. The union at a node is unique to that node in the multi-labelled tree (with one exception near the root in the no-diploids case). Unions can therefore be used to identify nodes. In the species network, the identity of the sequence is lost, but a similar mechanism is used.

A **MNL move** is a MCMC move for trees based on the ideas of Mau, Newton and Larget (1999). Similar moves are used in *BEAST. The tree is randomly oriented (so all nodes ordered left to right), a random internal node is chosen and its height altered, then the tree is reconstructed.

1.2 Network structure

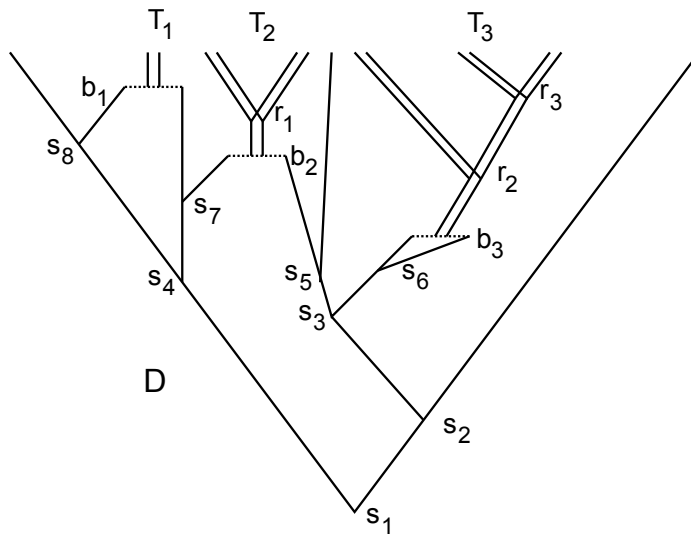


Figure 1.1: Network structure: 4 diploids and 6 tetraploids in three subtrees

[History: For the single hybridization case, I had a simple tree for the diploids with fairly complicated legs in the (single) tetraploid tree specifying which diploid branches it joined to. I now divide the network up with more information in the diploid part, as described next.]

The species network is composed of one or more trees representing tetraploid (sub)trees, and a diploid history. The latter is a tree with some tips representing diploid species at present time and others representing the points at which hybridization (to form a tetraploid) occurs. The latter are in pairs and have times before present, and I call them ‘hybridization tips’ or ‘hyb-tips’. From the point of view of a tetraploid tree these hyb-tips are feet at the ends of legs.

See Fig 1.1. Symbols $s_1 \dots s_8$ denote speciation nodes in the diploid history, $r_1 \dots r_3$ s denote speciation nodes in tetraploid subtrees, and b_1, \dots, b_3 indicate pairs of hybridization tips. D is the diploid history with 3 tips at present and 3 pairs of hyb-tips. There are three tetraploid subtrees T_1, T_2, T_3 with 1,2,3 tips respectively. s_5, s_6, s_7, s_8 are feet.

1.3 AlloppNET formula

1. W is the network topology and node times. The multi-labelled tree derived from it is M_W .
 2. θ is the population parameters. See [2012-08-06-popvalues-to-nodes.pdf](#) for details.
 3. λ is the parameters for W , that is, the topology and node times. λ could consist of a speciation rate, an extinction rate, and a hybridization rate.
 4. η is the population scaling factor, appearing in a hyperprior for θ
 5. n is the number of gene trees.
 6. τ_i is the i 'th gene tree topology and node times.
 7. α_i is all the other parameters belonging to the i 'th gene tree: parameters for site rate heterogeneity, substitution model, branch rate model, root model.
 8. g_i is (τ_i, α_i) , that is, all the parameters for the i 'th gene tree.
 9. γ_i is the permutations of sequences within individuals for the i 'th gene.
 10. d_i is the sequence data for the i 'th gene.
- $\tau = (\tau_1, \dots, \tau_n)$, and similarly for α, g, γ, d .

$$\Pr(W, \theta, g, \gamma | d) \propto \Pr(W | \lambda) \Pr(\lambda) \times \tag{1.1}$$

$$\Pr(\theta | \eta) \Pr(\eta) \times \tag{1.2}$$

$$\Pr(\gamma) \times \tag{1.3}$$

$$\prod_i \Pr(\tau_i | M_W, \theta, \gamma_i) \times \tag{1.4}$$

$$\prod_i \Pr(d_i | g_i) \tag{1.5}$$

1. $\Pr(W | \lambda) \Pr(\lambda)$ is the network prior: the probability of W before seeing any molecular data.
2. $\Pr(\theta | \eta) \Pr(\eta)$ is the population prior.
3. $\Pr(\gamma)$ is the permutation prior. Quite likely uniform, so can be omitted.
4. $\Pr(\tau_i | M_W, \theta, \gamma_i)$ is the probability of τ_i , when permuted by γ_i , fitting into the multi-labelled tree M_W with populations determined by θ . Note that this probability does not depend on α_i . See below for what permuting τ_i by γ_i means.
5. $\Pr(d_i | g_i) = \Pr(d_i | \tau_i, \alpha_i)$ is the ‘Felsenstein likelihood’ of the data for the i 'th gene given the i 'th gene tree.

I previously thought of

$$\Pr(d_i | g_i, \gamma_i) \Pr(g_i | W, \theta)$$

as

$$\Pr(\gamma_i(d_i)|g_i) \Pr(g_i|W)$$

so that the γ_i are thought of as permuting the sequence data d_i . This doesn't work well in implementation in BEAST: lots of existing code does not expect sequences to be swapped around. It would be possible to regard the γ_i as specifying a topological change in a gene tree (eg two terminal branches would be swapped). However, it seems simplest to regard γ_i as permuting the tip labels of the gene tree. The sequences attached to a tip don't change, nor does the gene tree topology. Instead, the way in which the sequences are assigned tips in the multi-labelled tree W is changed. Thus one can write:

$$\Pr(\tau_i|W, \theta, \gamma_i) = \Pr(\gamma_i(\tau_i)|W, \theta)$$

Chapter 2

Overall code structure of AlloppNET

List of classes, and tests.

2.1 List of classes

2.1.1 Parsers in `dr.evomodelxml.operators`

- `AlloppChangeNumHybridizationsParser`
- `AlloppHybPopSizesScaleParser`
- `AlloppNetworkNodeSlideParser`
- `AlloppSequenceReassignmentParser`

2.1.2 Parsers in `dr.evomodelxml.speciation`

- `AlloppMSCoalescentParser`
- `AlloppNetworkPriorModelParser`
- `AlloppNetworkPriorParser`
- `AlloppSpeciesBindingsApSpInfoParser`
- `AlloppSpeciesBindingsIndividualParser`
- `AlloppSpeciesBindingsParser`
- `AlloppSpeciesNetworkModelParser`

2.1.3 Classes in `dr.evomodel.operators`

- `AlloppChangeNumHybridizations` An operator which changes the number of tetraploid subtrees by split and merge operations.
- `AlloppHybPopSizesScale` An operator which changes the sizes of populations just after hybridization.
- `AlloppNetworkNodeSlide`. An operator which changes node heights and possibly tree topology within a tetraploid tree or diploid history or changes hybridization times.
- `AlloppSequenceReassignment` An operator which changes assignments of sequences within an individual

2.1.4 Classes in `dr.evomodel.speciation`

- `AlloppDiploidHistory` represents the part of the network before hybridizations. It is basically a tree with some tips representing diploid species at present time and others representing the points at which hybridization occurs.
- `AlloppLeggedTree` is a homoploid ‘tree with legs’. Used only for tetraploid trees (July 2012).
- `AlloppNode` An interface implemented by `DipHistNode` in `AlloppDiploidHistory`, `TetraTreeNode` in `AlloppLeggedTree`, and `MulLabNode` in `AlloppMulLabTree`. The ABC `AlloppNode.Abstract` contains some common functionality, especially for constructing `AlloppDiploidHistory`, `AlloppMulLabTree`.
- `AlloppMSCoalescent` computes coalescent log-likelihood of a set of gene trees embedded inside a allopolyploid species network. It is an `instanceof Likelihood`.
- `AlloppMulLabTree` implements a multi-labelled binary tree. Its nodes can store populations and hybridization times. It made from the tetraploid trees and diploid history.
- `AlloppNetworkPrior` computes log-likelihood of prior for the network. It is an `instanceof Likelihood`.
- `AlloppNetworkPriorModel` stores parameters for network prior (eg rates). It is an `instanceof Model`.
- `AlloppSpeciesBindings` knows how species are made of individuals and individuals are made of taxa (= diploid genomes within individuals). It is an `instanceof Model`.
- `AlloppSpeciesNetworkModel` implements the species network as a collection of ‘tree with legs’, that is, `AlloppLeggedTree`’s , and converts this representation into a multi-labelled binary tree, that is, an `AlloppMulLabTree`. It is an `instanceof Model`.

2.1.5 Classes in `dr.evolution.tree`

- `SlidableTree` An interface implemented by `AlloppDiploidHistory`, `AlloppLeggedTree`. It is a minimal tree interface that supports MNL moves.

2.1.6 Classes in `test.dr.evomodel.speciation`

- `AlloppSpeciesNetworkModelTEST` is for testing.

2.1.7 Classes in `dr.util`

- `AlloppMisc` is odds and ends, mainly for testing.

2.2 Tests

JUnit tests are in `AlloppSpeciesNetworkModelTEST`. I have decided to create a new (inner) class for each test, which is passed to constructors and other functions. This distinguishes test code from normal code, and sometimes the class is used to supply extra information needed for the test. In other cases it looks messy.

2.2.1 Test 1: network to MUL-tree

I have code for translating a network representation into a mullab representation, which is tested by some small cases in a test unit `AlloppSpeciesNetworkModelTest`. That does 3 tetra species, and 2 diploid species, in various arrangements.

2.2.2 Test 2: Likelihood of MUL-tree

Builds a small `AlloppMulLabTree`, with every height, coalescence, nlineages, flags, unions filled in, mostly ‘manually’. Filling population indices and calculation of likelihood is then done as in real usage. The result is compared to that calculated by R code.

Chapter 3

Interfaces and classes in AlloppNET

The next two sections describe two interfaces. The remaining sections describe the major classes. They are in order of packages, and alphabetically within packages.

3.1 Interface AlloppNode

In `evomodel.speciation`.

Implemented by `MullabNode`, `TetraTreeNode`, `DipHistNode` which both extend `AlloppNode.Abstract`.

`nofChildren()`, `getChild(int ch)`, `getAnc()` `getTaxon()` `getHeight()`, `getUnion()`. These are all get methods.

`setChild()` `setAnc()`, `setTaxon()`, `setHeight()`, `setUnion()`, `addChildren()`. These are all set or simple edit methods.

`String asText()`. For debugging output.

`fillinUnionsInSubtree(AlloppSpeciesBindings apsp)`. Recursive. If node has children, it calls itself on both children, then makes this node have clade equal to the union of the clades of its two children. If tips are filled, calling this on root does whole tree.

`nodeOfUnionInSubtree(FixedBitSet x)`. Searches subtree rooted at node for most tipward node whose union contains x. If x is known to be a union of one of the nodes, it finds that node, so acts as a map union to node.

`AlloppNode.Abstract` implements the last two. It also has a static method:

`subtreeAsText()`. For debugging output.

3.2 Interface SlidableTree

In `evolution.tree`.

Provides implementation of MNL move. The moves are applied to tetratrees as `AlloppLeggedTrees` and the `DiploidHistory`.

3.2.1 Interface Methods

`getSlidableRoot()`, `getSlidableNodeCount()`, `getSlidableNodeTaxon()`,
`getSlidableNodeHeight()`, `setSlidableNodeHeight()`, `isExternalSlidable()`,
`getSlidableChild()`, `replaceSlidableChildren()`, `replaceSlidableRoot()`.

3.2.2 Methods (static utils)

`mauCanonical()`. Returns a left-right ordering of nodes with randomly flipped children.

`mauReconstruct()`. Makes a new tree after a node height has changed.

Private:

`mauCanonicalSub()`. Recursive, for `mauCanonical()`.

`mauReconstructSub()`. Recursive, for `mauReconstruct()`.

`highestNode()` For `mauReconstruct()`.

3.3 Operator AlloppChangeNumHybridizations

In `evomodel.operators`.

Operator which changes the number of tetraploid trees. See [2012-09-24-MCMCmoves.pdf](#) for details of the algorithm.

It contains two simple private classes `SplitCandidate` and `MergeCandidate` for listing possible moves and choosing one.

3.3.1 Methods

Implements standard simple methods for operator. The key one is `doOperation()` which calls either `doMergeMove()` or `doSplitMove()`.

`doMergeMove()` uses `findCandidateMerges()` to list possible merges, chooses a random one and calls `mergeTettreePair()` to carry it out. Calls `removeHybPopParam()` in `AlloppSpeciesNetworkModel`. Calculates and returns Hastings ratio.

`doSplitMove()`. uses `findCandidateSplits()` to list possible splits, chooses a random one and calls `splitTettree()` to carry it out. Calls `addHybPopParam()` in `AlloppSpeciesNetworkModel`. Calculates and returns Hastings ratio.

`findCandidateMerges()`, `countCandidateMerges()` for `doMergeMove()`, latter for Hastings ratio.

`findCandidateSplits()`, `countCandidateSplits()` for `doSplitMove()`, latter for Hastings ratio.

`pairAreMergeable()` checks topology of legs in diploid history agree and meet in the way that is produced by a split move, Done using `tettreesShareLegs()` in `AlloppDiploidHistory`.

`mergeTettreePair()` merges two tetraploid trees by calling a constructor in `AlloppLeggedTree`, fixes up the links to diploid history, then calls `removeFeet()` in `AlloppDiploidHistory` to make a smaller diploid history. See PDF mentioned above for more details.

`splitTettree()` splits a tetraploid tree. It is passed two nodes which were children of root of old tree and which become the roots of the two new ones. It makes two calls to a constructor in `AlloppLeggedTree` to make the new trees. It calls `addTwoDipTips()` in `AlloppDiploidHistory` to make a larger diploid history. See PDF mentioned above for more details.

3.4 Operator `AlloppHybPopSizesScale`

This is a simple scaling operator which scales a single randomly chosen population size just after hybridization. Can't use the standard `scaleOperator` because the number of such population sizes changes.

3.5 Operator `AlloppNetworkNodeSlide`

In `evomodel.operators`.

Extension of ideas of Mau et al (1999) to deal with allopolyploid networks. It is three operators in one:

- Change a hybridization height
- Slide a node in a tetraploid tree
- Slide a node in a diploid tree

It contains a simple private class `NodeHeightInNetIndex` for recording a chosen node/move type.

3.5.1 Methods

Implements standard simple methods for operator. The key one is `doOperation()` which calls `operateOneNodeInNet()`.

Private:

`randomnode()`. Chooses a random node in network, which can mean a node in the diploid history, a node in a tetraploid subtree or a hybridization event.

`operateOneNodeInNet()`. Calls `randomnode()` then one of `operateOneNodeInTetraTree()` or `operateHybridHeight()` or `operateOneNodeInDiploidHistory()`.

`operateHybridHeight()`. Moves the hybridization height to somewhere between root of tree and split height or most recent foot height. This means changing the heights of a pair of hyb-tips in parallel.

`operateOneNodeInTetraTree()`. Does a MNL move. It avoids moving the root before the hybridization height as well as respecting limits from gene trees. It calls `SlidableTree.Utls.mauCanonical()` and `SlidableTree.Utls.mauReconstruct()`.

`operateOneNodeInDiploidHistory()`. Does a MNL move. It obeys three restrictions when choosing a new node height. It avoids making nodes so ancient that they become incompatible with any of the gene trees. It avoids making parent nodes of hyb-tips more recent than the hyb-tips. It keeps the root a diploid by preventing the root becoming to the left or right of all diploids, which can mean preventing the root becoming too recent, or another node becoming too ancient. It calls `SlidableTree.Utls.mauCanonical()` and `SlidableTree.Utls.mauReconstruct()`.

3.6 Operator `AlloppSequenceReassignment`

In `evomodel.operators`.

Operator which changes the assignment of sequences belonging to a randomly chosen individual in a randomly chosen species.

3.6.1 Methods

Implements standard simple methods for operator. The key one is `doOperation()` which does one of three types of move. The first two, `permuteOneSpeciesOneIndivForOneGene()`, and `permuteSetOfIndivsForOneGene()` are in `AlloppSpeciesBindings` and do ‘small’ and ‘big’ changes to sequence assignments within a gene tree. The third swaps a whole tetraploid subtree. It makes multiple calls to `flipAssignmentsForAllGenesOneSpecies()` in `AlloppSpeciesBindings` and `flipLegsOfTetraTree()` in `AlloppSpeciesNetworkModel`.

3.7 Diploid history `AlloppDiploidHistory`

In `evomodel.speciation`.

This a tree with some tips representing diploid species at present time and others representing the points at which hybridization (to form a tetraploid) occurs. The latter are in pairs and have times before present, and I call them ‘hybridization tips’ or ‘hyb-tips’. From the point of view of a tetraploid tree these hyb-tips are feet at the ends of legs.

The purpose of this class is to represent the part of the network before hybridizations (=‘diploid history’) in a form (the array of `DipHistNode`’s) that can be subjected to Mau-type moves.

The diploid history is constructed from a diploid tree and a single tetraploid tree initially. MCMC moves can change the number of tetraploid trees.

3.7.1 Inner classes

`DipHistNode` is a private class implementing `AlloppNode`. An array of these is used to represent the diploid history as a tree. It has fields for unions, and for linking hyb-tips to a `AlloppLeggedTree`.

3.7.2 Methods

`AlloppDiploidHistory()`. Main constructor for initial random state. Passed an array of taxa for the diploids, and a `AlloppLeggedTree` for the tetraploids, from which the `AlloppDiploidHistory` is made. This is an array of `DipHistNode`’s. The constructor also makes a `SimpleTree` representing the diploid history, for testing only.

There is a copy constructor.

There is another constructor for testing, which is built from an array of `SimpleNodes`, a set of tetraploid trees, and a `AlloppSpeciesBindings` (which is needed for making unions).

`getSlidableRoot()`, `replaceSlidableRoot()`, `getSlidableNodeCount()`, `getSlidableNodeHeight()`, `\verbgetSlidableNodeTaxon()+`, `setSlidableNodeHeight()+`, `isExternalSlidable()`, `getSlidableChild()`, `replaceSlidableChildren()`. These are overrides for `SlidableTree` interface.

`asText()` for debugging.

`getInternalNodeCount()` for node slide operator.

`getDiploidTipCount()` used to construct `AlloppMullabTree`.

`collectFeet()` used by move hyb height operator.

`tipIsDiploidTip()` used by node slide operator for keeping a diploid root.

`tettreesShareLegs()` for move that merges two tettees.

`intervalOfFoot()` is for move that merges two tettees. This is for Hastings ratio calculation.

`removeFeet()` is for move that merges two tettees. This is for after merge.

`addTwoDipTips()` is for move that splits a tettee. This is for after split.

`getAncHeight()` is for move that splits a tettee.

`getRootIndex()`, `getHeightFromIndex()`, `getLftFromIndex()`, `getRgtFromIndex()`, `getTaxonFromIndex()` are for `AlloppMullabTree` constructor.

`getRootHeight()`

`getHybHeight()`

`collectInternalAndHybHeights()` for prior lhood.

`moveHybridHeight()` for move.

`scaleAllHeights()` Passed a scaling factor this multiplies all heights (including those of hyb-tips) in the tree. For move and network construction.

`clearAllNodeTettree()` for tests during merging tettees.

`getNodeTettree()` for moving hyb time, and tests during merging tettees.

`getNodeLeg()` for node slide in diploid history, for unions, for gene-tree checking.

`setNodeTettree()` is for move that merges two tettees.

`diphistTreeAsText()`, `diphistTreeAsUniqueNewick()`, `diphistTreeAsNodeList()`. Output for testing.

`diphistOK()` for internal consistency checks.

Private:

`buildSubtreeFromNodes()` for merging and splitting moves, when diploid history size changes.

`removeTip()` for `removeFeet()`.

`makesimpletree()`. For testing, used by constructor.

`makesimplesubtree()`. For `makesimpletree()`.

`simpletree2dhtesttree()` for unit test construction.

3.8 Homoploid tree model `AlloppLeggedTree`

In `evomodel.speciation`.

This is a ‘tree with legs’, which is used for a tetraploid species tree which is attached to a diploid history via its legs.

3.8.1 Inner classes

`ALTNode` is a private class implementing `AlloppNode` used to represent a tree, in a way that supports MNL moves. Used for the tetraploid trees, and maybe one day for hexaploids. It has a union field, used for calculations to restrict MCMC moves to be compatible.

3.8.2 Methods

`AlloppLeggedTree()`. Main constructor for initial random state. Passed an array of Taxons. Makes a random Yule-type tree for them, as an array of `ALTNodes`. The legs are unset at this point.

There is a copy constructor for store and restore methods.

There is a constructor which makes a merged tree from two trees, for merge move.

There is a constructor which makes a tree from a subtree of a given tree, for split move.

There is also a constructor for testing, which make small nonrandom trees.

`getSlidableRoot()`, `replaceSlidableRoot()`, `getSlidableNodeCount()`,
`getSlidableNodeHeight()`, `\verbgetSlidableNodeTaxon()+`, `setSlidableNodeHeight()+`,
`isExternalSlidable()`, `getSlidableChild()`, `replaceSlidableChildren()`. These are
overrides for `SlidableTree` interface.

`asText()` for debugging.

`leggedtreeOK()` for internal consistency checks.

()

`scaleAllHeights()`. Passed a scaling factor this multiplies all heights in the tree. For moves and network construction.

`fillinTipUnions()` for `unionOfWholeTetTree()` in `AlloppSpeciesNetworkModel`.

`getRootHeight()` returns what it says.

`getExternalNodeCount()`, `getInternalNodeCount()` return what they say.

`collectInternalHeights()` returns what it says, for prior likelihood calculation.

`setDiphistLftLeg()`, `setDiphistRgtLeg()` used by diploid history constructor and moves to change legs.

`getDiphistLftLeg()`, `getDiphistRgtLeg()` return what they say.

Private:

`copySubtree()` for ‘merge’ constructor.

`noftipsSubtree()` for ‘subtree’ constructor.

`randomnodeheight()` for initial constructor.

3.9 Likelihood calculator `AlloppMSCoalescent`

In `evomodel.speciation`.

Computes coalescent log-likelihood of a set of gene trees embedded inside a allopolyploid species network.

3.9.1 Methods

`AlloppMSCoalescent()`. Constructor. Stores `AlloppSpeciesBindings` and `AlloppSpeciesNetworkModel` and adds itself to their model-listeners.

There is also a constructor for testing.

Implements standard simple methods for likelihood. Key ones follow.

`calculateLogLikelihood()`. Calls `geneTreeFitsInNetwork` and `geneTreeLogLikelihood` in `AlloppSpeciesBindings` for each gene.

`getLikelihoodKnown()`. Returns false. Always recalculate from scratch.

3.10 Multi-labelled tree `AlloppMulLabTree`

In `evomodel.speciation`.

Represents the species network as a single binary tree with tips that can be multiply labelled with species. It is reconstructed when the network changes. It is ‘refilled’ with information about coalescences in order to calculate the likelihood $\Pr(\tau_i|W, \theta, \gamma_i)$.

It contains the population size parameters. These are three arrays, for tip populations, rootward populations, and hybrid populations.

3.10.1 Inner classes

`MulLabNode` implements `AlloppNode`. It contains information (‘node rôle flags’) about the node’s rôle in the network (in a tetraploid tree, the root of one, ancestral to one), populations sizes (via indices), and a union field which is a set of (species index, sequence index) pairs which identifies the node. It has fields for number of lineages, and for coalescent times, which are filled in for one gene at a time during likelihood calculation.

`SpSqUnion` - low level class used for mapping population values to nodes in `AlloppMulLabTree`.

`PopulationAndLineages` - records the information (times, populations, number of lineages) needed to calculate the probability of coalescences in a single branch of the `AlloppMulLabTree`.

3.10.2 Inner class methods

Apart from `AlloppNode` implementation, there is:

`MulLabNode.tippop()`, `MulLabNode.hybpop()`, `MulLabNode.rootpop()`. Returns the population value at the tip end of the branch, just after hybridization, or root end of the branch, respectively.

`PopulationAndLineages.populationAt()`. For calculating the probability of coalescences in a single branch of the multi-labelled tree.

3.10.3 AlloppMulLabTree Methods

`AlloppMulLabTree()`. Constructor. Passed a `AlloppDiploidHistory` and an array of `AlloppLeggedTree`'s, the `AlloppSpeciesBindings` and the population values. Makes a single multi-labelled binary tree. It counts tips, makes array of `MulLabNodes`. It calls `subtree2MulLabNodes()` to construct the topology with taxons and unions filled at tips, and set some node role flags. Then it calls `fillinUnionsInSubtree()`. Then `fillinTetraFlagsInSubtree()` completes the job of setting node role flags. Finally it calls `makesimpletree()` to make tree for output (so that `AlloppSpeciesNetworkModel` can implement `Tree` interface).

There is a constructor for testing conversion of diploid history plus tetraploid trees to MUL-tree.

There is a constructor for testing likelihood calculations.

`testGeneTreeInMULTreeLogLikelihood()` for testing.

`fillmInodesforLhoodtest1()` for testing.

`mullabtreeOK()` for internal consistency checks.

`mullabTreeAsNewick()`. Converts the multi-labelled tree to a Newick string, currently just for testing.

`asText()`. For testing.

`clearCoalescences()`. Removes coalescent information from nodes. Calls

`clearSubtreeCoalescences()`. The method for recording coalescences 'accumulates' them as they are found in gene trees, so need to remove them all first.

`recordLineageCounts()`. Fills in counts of lineages at nodes. Calls `recordSubtreeLineageCounts()`.

`coalescenceIsCompatible()`. See method of same name in `AlloppSpeciesNetworkModel`.

`recordCoalescence()`. See method of same name in `AlloppSpeciesNetworkModel`.

`sortCoalescences()`. See method of same name in `AlloppSpeciesNetworkModel`.

`geneTreeInMLTreeLogLikelihood()`. Calculates the log-likelihood for a gene tree in the multi-labelled tree. Calls `fillinpopvals()` and `geneTreeInMLSubtreeLogLikelihood()`.

Private:

`fillinTetraFlagsInSubtree()` for constructor.

`subtree2MulLabNodes()` for constructor. Visits nodes in diploid history recursively, and when it gets to a hyb-tip, it calls `allopptree2MulLabNodes()` to recurse into a tetraploid tree. Each tetraploid tree is visited twice, once for each hyb-tip. It thus builds the MUL-tree topology. Taxons and unions are set at tips. This also sets some `tetraancestor` flags and all `tetraroot` flags.

`allopptree2MulLabNodes()`. Visits nodes in a tetraploid tree recursively. Taxons and unions are set at tips. This also sets some `intetratree` flags.

`makesimpletree()`. Converts the multi-labelled tree into a `SimpleTree` so that it can be logged by standard tree logger.

`makesimplesubtree()`. Recursive. For `makesimpletree()`.

`subtreeAsText()`. Recursive. For `asText()`.

`nodeOfUnion()`. Passed `FixedBitSet x`, it returns the most tipward node whose union contains `x`. If `x` is known to be a union of one of the nodes, it finds that node, so acts as a map from union to node. Calls `nodeOfUnionInSubtree()`.

`clearSubtreeCoalescences()`. Recursive, for `clearCoalescences()`.

`recordSubtreeLineageCounts()`. Recursive, for `recordLineageCounts()`.

`fillinpopvals()`. This fills in indices in nodes to index values in the three population arrays. The population values are per-species-clade (per-branch in network), but of course more than one node in `MulLabTree` may correspond to the same species. Other complications are that tips are different from internal nodes, and that nodes which roots of tetratrees, ancestors of such roots, as well as the root are treated differently. It collects unions (which represent sets whose elements identify a species and a sequence) from the nodes and then sorts them so that sets of nodes with same species clade are grouped together. This does some of what is required, since nodes with the same species clade are treated the same. Calls `fillinpopvalsforspunion()` to deal with a set of nodes with same species clade. See [2012-08-06-popvalues-to-nodes.pdf](#) for more details.

`fillinpopvalsforspunion()`. For `fillinpopvals()`. Deals with a one union of species indices, that is, for all nodes in the multi-labelled tree which contain a particular group of species in thier clade.

`siblingOfNode()` is simple help function.

`geneTreeInMLSubtreeLogLikelihood()`. Recursive, for `geneTreeInMLTreeLogLikelihood()`. Calls `branchLLInMULtreeNoDiploids()` or `branchLLInMULtreeTwoDiploids()`.

`branchLLInMULtree()`. Likelihood calculation of gene tree in multi-labelled tree for one branch in the case of no diploids. This

`limbLogLike()`. A 'limb' is part or all of a branch in which the population varies linearly (no hybridization or other jumps). This is used by `geneTreeInMLSubtreeLogLikelihood()`.

`limbLinPopIntegral()`. For `limbLogLike()`.

`union2spseqindex(union)`. Passed union for a tip, hence only containing one (species index, sequence index) pair. It returns the index of that.

Comparator:

`SPUNION_ORDER.compare()`. For `fillinpopvals()`. This is quite a complex sort, see `fillinpopvals()`. Its main task is to sort the nodes (defined by clades of (species, sequence) pairs) so that nodes with the same species clades are grouped together. But it also sorts the groups so that tips occur first, and it sorts nodes within groups in a well-defined way that `fillinpopvalsforspunionNoDiploids()` and `fillinpopvalsforspunionTwoDiploids()` rely on. More detail follows.

The comparator sorts the unions of (species, sequence) pairs (`SpSqUnions`) so that all unions containing the same set of species (ignoring sequence) are grouped together. Call the sets of `SpSqUnions` for the same species a group. There can be 1,2 or 3 `SpSqUnions` in a group.

The groups are sorted in order of increasing number of species (clade size). All groups for a single species (a tip in the network) come first, then those groups for two species, and so on to the root for all species. For groups that have equal numbers of species, a lexicographical ordering using species indices is used.

Within each group, species and sequence information is used to sort the 1 to 3 `SpSqUnions`. The size of the ‘clade’ of (species, sequence) pairs is used first in the comparison, which ensures that the three nodes with the same species - corresponding to two roots of tetratrees in the multi-labelled tree plus a leg-join - are ordered so that the two roots come first.

3.11 Prior likelihood calculator `AlloppNetworkPrior`

In `evomodel.speciation`.

Computes prior log-likelihood of allopolyploid species network. This has two main components: for the topology and node times; and for the populations. (Unlike earlier versions of `AlloppNET`, the prior model on populations are specified as part of the network prior model, since the network needs to get hold of the distribution to generate new values when the number of hybridizations increases. Aug 2012.)

3.11.1 Methods

Implements standard simple methods for likelihood. Key ones follow.

Constructor gets the distribution model for hybrid populations from `AlloppNetworkPriorModel` and sets this in `AlloppSpeciesNetworkModel`.

`calculateLogLikelihood()`. Calls `loglikelihoodEvents()`, `loglikeNumHybridizations()` to calculate the prior for the topology and node times. Adds the priors for the population values via the distribution models in `AlloppNetworkPriorModel`.

`getLikelihoodKnown()`. Returns false. Always recalculate from scratch.

`loglikelihoodEvents()` is Yule-like likelihood using times of events.

`loglikeNumHybridizations()` is experimental adjustment.

3.12 Prior model `AlloppNetworkPriorModel`

In `evomodel.speciation`.

Constructed from two one-dimensional parameters, event rate and population scaling factor, and three distribution models, one for each set of population values (tip, rootward, hybrid). It just stores this stuff for `AlloppNetworkPrior` and `AlloppSpeciesNetworkModel`.

3.13 Connecting network to gene trees: AlloppSpeciesBindings

In `evomodel.speciation`.

`AlloppSpeciesBindings` knows how species are made of individuals and individuals are made of taxa (= diploid genomes within individuals).

It also contains the list of gene trees - tree topologies and node times, plus popfactors. Given a `AlloppSpeciesNetworkModel` it can say if a gene tree is compatible, and calculate the loglikelihood of the gene tree 'fitting' into the network.

It is here that assignments of sequence copies within individuals get permuted. See `GeneTreeInfo.AlignmentRowInfo` below.

3.13.1 Inner classes

`Individual` - Simple helper class for one individual containing one or more sequences.

`SpeciesIndivPair` - Simple helper class used by `permuteSetOfIndivs()` which is part of sequence reassignment operator.

`ApSpInfo` - Simple helper class for one (allopolyploid) species, containing one or more individuals

`GeneTreeInfo` - A gene tree as used by BEAST, plus popfactor, plus indices for each individual to map sequences to indices (0 or 1 for tetraploids) which identify the legs of the tetraploid subtree.

`GeneTreeInfo.SequenceAssignment` - where the indices just mentioned are stored.

`GeneTreeInfo.GeneUnionNode` - for `GeneUnionTree`.

`GeneTreeInfo.GeneUnionTree` - This is used during calculations `fitsInNetwork()`, `treeLogLikelihood()` for one gene tree at a time, then discarded. It serves a similar function to JH's `CoalInfo`, storing the set (=union) of species-sequence pairs belonging to a node in the gene tree. I copy gene tree topology and times into a `GeneUnionTree` to do calculations.

3.13.2 Methods

There are a lot of mapping of one kind of index or indices to others, one to get list of species at a given ploidy level, etc. `fitsInNetwork()` and `geneTreeLogLikelihood()` are key methods.

3.13.3 Methods for small inner classes

`ApSpInfo.taxonFromIndSeq()` Passed indices for individual, sequence, returns taxon.

`GeneTreeInfo.SequenceAssignment.toString()`. For header in log file.

`GeneTreeInfo.GeneUnionNode.asText()`. For testing.

3.13.4 GeneTreeInfo.GeneUnionTree methods

`GeneUnionTree()`. Constructor. Calls `genetree2geneuniontree()` to build the `GeneUnionTree`.

`getRoot()`. Does what it says.

private to `GeneUnionTree`:

`subtreeFitsInNetwork()` Recursive. Calls `coalescenceIsCompatible()` in network.

`subtreeRecordCoalescence()` Recursive. Calls `recordCoalescence()` in network.

`genetree2geneuniontree()` Recursive. Copies topology, fills in union fields.

`asText()`. For testing. Makes textual rep of `GeneUnionTree`.

`subtreeAsText()`. For `asText()`.

3.13.5 GeneTreeInfo methods

`GeneTreeInfo()`. Constructor. Fills array of `AlignmentRowInfo` s. Fills int array of lineage counts at tips.

`seqassignsAsText()`. For testing.

`genetreeAsText()`. For testing.

`fitsInNetwork()`. Calls `subtreeFitsInNetwork()` in `GeneUnionTree`.

`treeLogLikelihood()`. Calls `clearCoalescences()` in network, makes new `GeneUnionTree`, calls `subtreeRecordCoalescence()` in `GeneUnionTree`, then `sortCoalescences()` in network, then `recordLineageCounts()` in network, and finally `geneTreeInNetworkLogLikelihood()` in network.

`storeSequenceAssignments()`. Stores sequence assignments.

`restoreSequenceAssignments()`. Restores stored sequence assignments.

`spseqUpperBound()`. Passed two sets of species-sequences, it finds the most recent coalescence for this gene such that the children of this gene in the gene tree contain at least one species-sequence from each set. Used by `AlloppNetworkNodeSlide`.

`permuteOneSpeciesOneIndiv()`. Chooses a random species and a random individual, and calls `permuteOneAssignment()`.

`permuteSetOfIndivs()`. Chooses a set of (species, individual) pairs, and calls `permuteOneAssignment()`. 2011-08-12: How it chooses the set is odd. Probably need revisiting when more testing of MCMC efficiency done.

`getSeqassigns()`. Passed taxon index, it returns (reference to) a `SequenceAssignment`. Used by logger.

`wasChanged()`. Does nothing. (Might set dirty flag one day.)

Private:

`collectIndivsOfNode()`. Used by `permuteSetOfIndivs()`.

`subtreeSpseqUpperBound()`. Called by `speciationUpperBound()` to do the real work.

`flipOneAssignment()`. Passed indices for a species and an individual, to do one ‘flip’ of a sequence assignment.

`flipAssignmentsForSpecies()`. Passed index for a species and calls `flipOneAssignment()` for all individuals.

3.13.6 AlloppSpeciesBindings methods

`AlloppSpeciesBindings()`. Constructor. Made from array of `ApSpInfos`, array of `TreeModels`, array of `popFactors`, and `minheight`. Makes ‘flattened’ arrays of species, individuals, taxa, sets up maps of indices. Makes array of `GeneTreeInfos` from `TreeModels` and `popFactors`, and then fixes the node heights to at least `minheight`.

There are also two constructors for testing.

`initialMinGeneNodeHeight()`. Returns what it says. Used for starting state of network.

`speciesseqEmptyUnion()` makes a union of the right size.

`taxonseqToTipUnion()` makes a union for a tip node, from the taxon.

`spsunion2spunion()`. Converts a set (a union) containing (species index, sequence index) pairs into a set containing just species indices.

`numberOfGeneTrees()`. Returns what it says.

`maxGeneTreeHeight()`. Returns what it says. Used for $\Pr(g_i|S)$ calculation in root.

`geneTreeFitsInNetwork()`. Passed index of a gene tree, it calls `fitsInNetwork()` in a `GeneTreeInfo`.

`geneTreeLogLikelihood()`. Passed index of a gene tree, it calls `treeLogLikelihood()` in a `GeneTreeInfo`.

`numberOfSpecies()`. Returns what it says.

`apspeciesName()`. Passed index of a species, returns what it says.

`SpeciesWithinPloidyLevel()`. Passed a ploidy level, it returns an array of `Taxons` for species.

`spandseq2spseqindex()`. Converts a (species index, sequence index) pair into a single index.

`spseqindex2sp()`, `spseqindex2seq()`. Inverse of above, they convert a single index into a (species index, sequence index) pair. They call `spseqindex2spandseq()`.

`apspeciesId2index()`. Species name to index.

`apspeciesId2speciesindiv()`. Converts a species id (name like 03_d_B) to a pair of indices (species, indiv). (Loosely, 03_d_B \rightarrow (d,03)). used by `permuteSetOfIndivs()`.

`numberOfSpSeqs()`. Returns number of (species index, sequence index) pairs.

`nLineages()` Passed index of a species, returns lineage count at tip.

`spseqUpperBound()`. Calls method of same name (which see) in each `GeneTreeInfo` to find minimum.

`permuteOneGeneOneSpeciesOneIndiv()`. Chooses a random gene and calls `permuteOneSpeciesOneIndiv()` on it.

`permuteSetOfIndivsForOneGene()`. Chooses a random gene and calls `permuteSetOfIndivs()` on it.

`flipAssignmentsForAllGenesOneSpecies()`. For all gene trees, this calls `flipAssignmentsForSpecies()` on it.

`seqassignsAsText()`. Calls method of same name (which see) in one `GeneTreeInfo`.

`genetreeAsText()`. Calls method of same name (which see) in one `GeneTreeInfo`.

`handleModelChangedEvent(Model model, Object object, int index)`. Calls `wasChanged()` on each gene tree.

`handleVariableChangedEvent(Variable variable, int index, ChangeType type)`. Never called. (asserts false.)

`storeState()`. Calls `storeGeneTreeState()` on each `GeneTreeInfo`.

`restoreState()`. Calls `restoreGeneTreeState()` on each `GeneTreeInfo`.

`acceptState()`. Does nothing.

`getColumns()`. Returns array of `LogColumn`'s for logger, for logging sequence assignments. One column for each (gene,taxon) pair.

Private:

`spseqindex2spandseq()`. Used by `spseqindex2sp()`, `spseqindex2seq()`.

3.14 Central class `AlloppSpeciesNetworkModel`

In `evomodel.speciation`.

This is the 'main' class for the allopolyploid model. It contains two representations of the network. It implements the species network as a collection of 'trees with legs' and converts this representation into a multi-labelled binary tree. The general idea is that the network is easiest to change (eg detach and re-attach tetraploid subtrees) while likelihood calculations are easiest to do in the multi-labelled tree.

The individual 'trees with legs' are implemented by a `AlloppDiploidHistory` and one or more `AlloppLeggedTree`'s. The representation as a multi-labelled binary tree is implemented by `AlloppMullabTree`. It contains a reference to `AlloppSpeciesBindings`. There is much communication between these classes.

This class extends `AbstractModel` and implements `Scalable`, `Units`, `Citable`, `Tree`, `TreeLogger.LogUpon`. The `Tree` interface is really an interface for the multi-labelled tree (`AlloppMulLabTree`). I think this is necessary because the tree logger (I presume) needs a constant reference whereas the multi-labelled tree comes and goes.

3.14.1 Methods

`AlloppSpeciesNetworkModel()`. Constructor. Made from an `AlloppSpeciesBindings`, and three starting values for populations. It gets the taxa, diploids and tetraploids, from the `AlloppSpeciesBindings` and calls `makeInitialNDipsNTetsNetwork()` to make a random network. It then scales it to be shorter than `apsp.initialMinGeneNodeHeight()` to fit the gene trees. It makes three arrays for populations (tips, rootward, hybrid population values). The first two are `Parameters` of the right size, but the hybrid population values are stored in an array of doubles because the dimensionality changes. A `Parameter` is constructed from this as required for output. Then it converts the network representation into a multi-labelled tree, by constructing an `AlloppMulLabTree`.

There is also a constructor for testing the conversion of network to multree.

`setHybPopModel()`. This is called from `AlloppNetworkPrior` (which is created after network) to supply a `ParametricDistributionModel` for the prior on the hybrid population values. It completes the construction of the network.

`getCitations()`. Returns citation info for display.

`alloppspeciesnetworkOK()` for internal consistency checks.

`mullabTreeAsText()`. For testing. Calls `asText()` in `AlloppMulLabTree`.

The next bunch are `AbstractModel` overrides.

`handleModelChangedEvent()`. Calls `fireModelChanged()`.

`handleVariableChangedEvent()`. Does nothing.

`protected void storeState()`. Makes copies of all homoploid trees in network. Makes copy of hybrid population values.

`protected void restoreState()` Restores copies of all homoploid trees in network. Restores copy of hybrid population values. Remakes multi-labelled tree. Remakes `Parameter` for hybrid population values.

`protected void acceptState()`. Does nothing.

`toString()`. For debugging logger. Calls `asText()` in `AlloppDiploidHistory`, `AlloppLeggedTree`, `AlloppMulLabTree` and `genetreeAsText()` and `seqassignsAsText()` in `AlloppSpeciesBindings`.

`getColumns()`. For debugging logger.

The next bunch are used by MCMC operators (`scale()` is a MCMC operator).

`beginNetworkEdit()`. Called before MCMC operation. Currently just debug checks.

`endNetworkEdit()`. Called after MCMC operation. Remakes `Parameter` for hybrid population values, remakes multi-labelled tree and calls `fireModelChanged()`.

`getName()`. Returns model name. (For `Scalable` implementation.)

`scale()`. For `Scalable` implementation, this stretches/squeezes whole network. Calls `scaleAllHeights()` and `scaleAllPopValues()`.

`calculateDipHistTipUnion()` finds the union of a tip (diploid or hyb-tip) in the diploid history. Used by move that slides node in diploid history to check gene-tree compatibility.

`addHybPopParam()`. Adds a new hybrid population value, sampled from the prior distribution set by `setHybPopModel()`. Returns the logarithm of the prior density, evaluated at the newly created value, for Hastings ratio calculations.

`removeHybPopParam()`. Removes a hybrid population value. Returns the logarithm of the prior density, evaluated at the value that has disappeared, for Hastings ratio calculations.

`getNumberOfTetraTrees()`. Returns number of tetraploid trees.

`getNumberOfInternalNodesInTetTree()`. Passed index, returns the number of internal node heights in a `AlloppLeggedTree` in the network.

`getNumberOfInternalNodesInDipHist()`. returns the number of internal node heights in the diploid history (not hyb-tips).

`getTetraploidTree()`. Passed index, returns a tree in the network.

`getDiploidHistory()` returns the diploid history.

`setTetTree()` for merge/split operators.

`addTetree()` for merge/split operators.

`removeTetree()` for merge/split operators.

`maxNumberOfHybPopParameters()`.

`setOneHybPopValue()`.

The next bunch are for likelihood calculations.

`getTipPopValues()`

`getRootPopValues()`

`getOneHybPopValue()`

`coalescenceIsCompatible()`. Passed a gene coalescence height and union. Called from `AlloppSpeciesBindings` to check if a node in a gene tree is compatible with the network. Calls function of same name in `AlloppMulLabTree` to do the calculation.

`clearCoalescences()`. Called from `AlloppSpeciesBindings` to remove coalescent information from branches of mullabtree. Calls function of same name in `AlloppMulLabTree` to do the work.

`recordCoalescence()`. Called from `AlloppSpeciesBindings` to add a node from a gene tree to its branch in mullabtree. Calls function of same name in `AlloppMulLabTree` to do the work.

`sortCoalescences()`. Sorts coalescences within each branch of the multi-labelled tree. Calls function of same name in `AlloppMullabTree` to do the work.

`recordLineageCounts()`. Records the number of gene lineages at nodes of the multi-labelled tree. Calls function of same name in `AlloppMullabTree` to do the work.

`geneTreeInNetworkLogLikelihood()`. Calculates the log-likelihood for a single gene tree in the network. Requires that `clearCoalescences()`, `recordCoalescence()`, `recordLineageCounts()` called to fill mullabtree with information about a particular gene tree's coalescences first. Calls function of same name in `AlloppMullabTree` to do some of the work.

Private:

`unionOfWholeTetTree()` for `calculateDipHistTipUnion()`.

`makeInitialNDipsNTetsNetwork()`. For constructor of initial random state.

`makeLoggingHybPopParam()`.

`scaleAllPopValues()`. Stretches or squashes all population values.

`scaleAllHeights()`. Scales all heights by calling method of same name in each `AlloppLeggedTree`. Used by constructor and by `scale` operator.

`numberOfTipPopParameters()`. Calculates the number of tip pop parameters.

`numberOfRootPopParameters()`. Calculates the number of rootward pop parameters.

Delegations for Tree:

`getRoot()`, `getNodeCount()`, `getNode(int i)`, `getInternalNode(int i)`,
`getExternalNode(int i)`, `getExternalNodeCount()`, `getInternalNodeCount()`,
`getNodeTaxon(NodeRef node)`, `hasNodeHeights()`, `setNodeHeight(NodeRef node)`,
`hasBranchLengths()`, `getBranchLength(NodeRef node)`, `getNodeRate(NodeRef node)`,
`getNodeAttribute(NodeRef node, String name)`, `getNodeAttributeNames(NodeRef node)`,
`isExternal(NodeRef node)`, `isRoot(NodeRef node)`, `getChildCount(NodeRef node)`,
`getChild(NodeRef node, int j)`, `getParent(NodeRef node)`, `getCopy()`, `getTaxonCount()`,
`getTaxon(int taxonIndex)`, `getTaxonId(int taxonIndex)`, `getTaxonIndex(String id)`,
`getTaxonIndex(Taxon taxon)`, `asList()`,
`getTaxonAttribute(int taxonIndex, String name)`, `iterator()`, `getUnits()`,
`setUnits(Type units)`, `setAttribute(String name, Object value)`,
`getAttribute(String name)`, `Iterator<String> getAttributeNames()`,
`addTaxon(Taxon taxon)`, `removeTaxon(Taxon taxon)`,
`setTaxonId(int taxonIndex, String id)`,
`setTaxonAttribute(int taxonIndex, String name, Object value)`,
`addMutableTaxonListListener(MutableTaxonListListener listener)`

Testing:

`testExampleNetworkToMulLabTree()`. Builds arrangements of trees with legs to test conversion to the multi-labelled tree.

`addSimpleNodeChildren()` for test cases.